



Workshop: Paternity and kinship testing including X-chromosomal markers

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First lecture: Genetical and statistical background

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ISFG workshop, Sep 3-4 2018, Catanzaro (Calabria), Italy,
<http://familias.name/isfg-kinship-2018/>

Program: Lectures and exercises

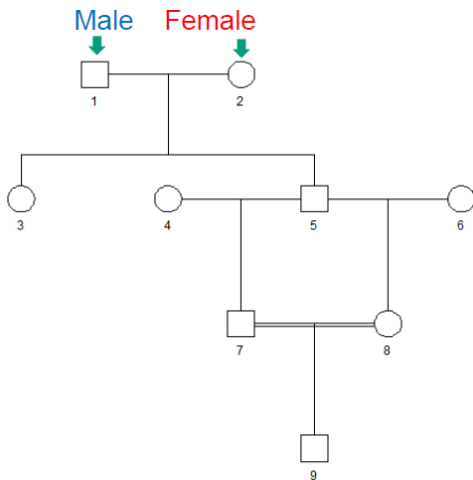
`http://familias.name/isfg-kinship-2018/`

Contents 09:15–10:00 and 10:15–11:30

- ▶ Basic forensic genetics very briefly:
 - Mendelian inheritance
 - Markers: autosomal, X, Y, mtDNA, STR-s.
- ▶ Weight of evidence. Likelihood Ratio (LR). Assumptions.
- ▶ Combining information. Bayes theorem
- ▶ Complications:
 - Mutation.
 - Theta correction.
 - Silent alleles.
- ▶ Introduction to Familias



Pedigree



Genetic markers I

- Small parts of the genome which ...

- have known position
- vary in the population
- are easy to genotype

allele =
a manifestation
of a variable locus

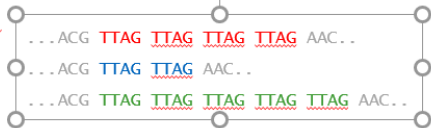
- SNPs (single nucleotide polymorphisms)

- two alleles
- usual requirement: $MAF > 1\%$ $MAF = \text{minor allele frequency}$
- very common in the genome (millions!)
- used in medical genetics +++

...CCGTTATATGGC...
...CCGTTAGATGGC...
...CCGTTATATGGC...
...CCGTTATATGGC...
...TTTATGATGGC...

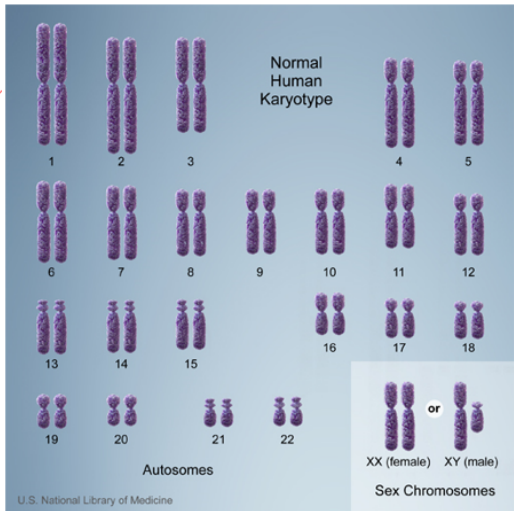
- STRs (short tandem repeats) = microsatellites

- consecutive repeats of 2-5 bases
- multiallelic: 5 - 50 alleles
- allele names: # repeats
- used in forensics



Genetic markers II

- chrom 1 - 22:
 - called the autosomes
 - all have 2 alleles at each locus
 - autosomal markers
- X chromosome
 - males have 1 allele
 - females have 2
 - X-linked markers
- Y chromosome
 - males have 1 allele
 - females 0
 - Y-linked markers



Genetic markers III. Example: Fusion 6C

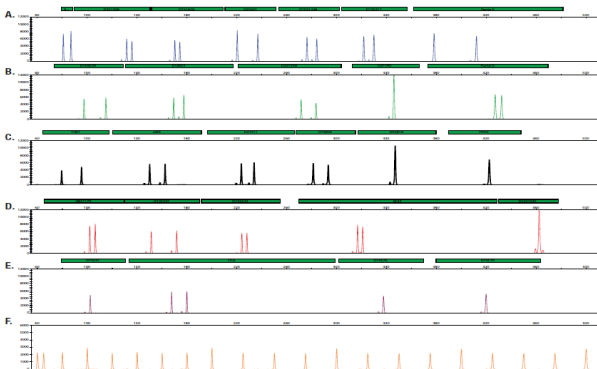


Figure 27. The PowerPlex® Fusion 6C System. The 2800M Control DNA (1.0ng) was amplified using the PowerPlex® Fusion 6C System and 29 cycles. Amplification products were mixed with WEN Internal Lane Standard 500 and analyzed using an Applied Biosystems® 3500xL Genetic Analyzer and a 1.2kV, 24-second injection. Results were analyzed using GeneMapper® ID-X software, version 1.4. **Panel A.** An electropherogram showing the peaks of the FL-6C-labeled loci: Amelogenin, D3S1358, D18S1656, D2S441, D10S1248, D13S317 and Penta E. **Panel B.** An electropherogram showing the peaks of the JOE-6C-labeled loci: D16S539, D18S51, D2S1338, CSF1PO and Penta D. **Panel C.** An electropherogram showing the peaks of the TMR-6C-labeled loci: TH01, vWA, D21S11, D7S820, D5S818, and TPOX. **Panel D.** An electropherogram showing the peaks of the CXR-6C-labeled loci: D8S1179, D12S391, D19S433, SE33 and D22S1045. **Panel E.** An electropherogram showing the TOM-6C-labeled loci: DYS391, FGA, DYS576 and DYS570. **Panel F.** An electropherogram showing the 60bp to 500bp fragments of the WEN Internal Lane Standard 500.

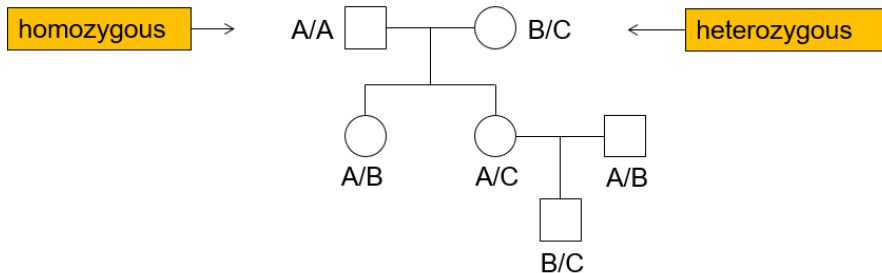
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Mendelian inheritance

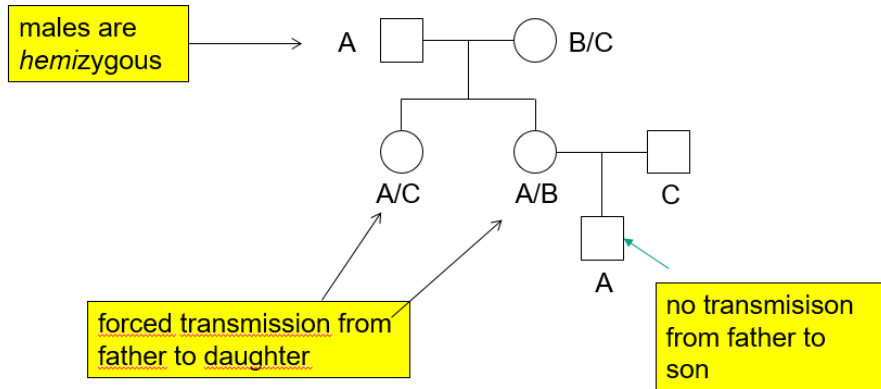
Example: autosomal marker with 3 alleles: A, B, C



Probability of transmitting either allele: **always 50%**

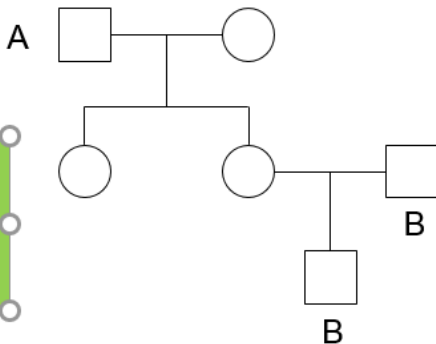
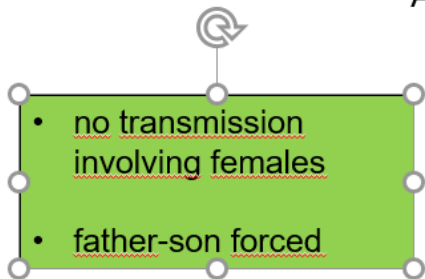
X linked inheritance

Example: X-linked marker with 3 alleles: A, B, C

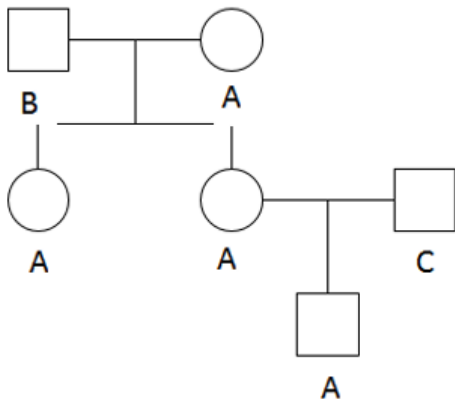


Y linked inheritance

Example: Y-linked marker with 2 alleles: A, B

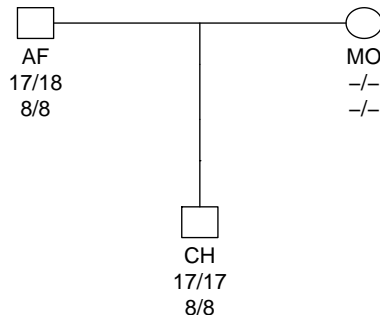


Mitochondrial (mtDNA) inheritance



Passed on from mother to all children

Hypotheses



- ▶ H_1 : AF **biological** father of CH.
- ▶ H_2 : AF and CH unrelated.
- ▶ Notation. Sometimes:
- ▶ $H_1 = H_P$:
“prosecution hypothesis” ,
- ▶ $H_2 = H_D$:
“defence hypothesis” .

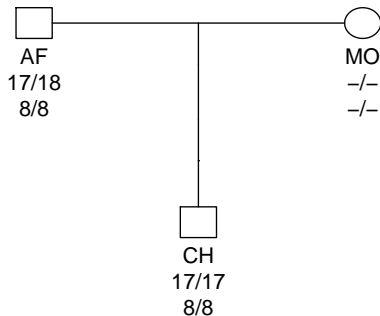
Likelihood ratio. Definition

Forensic framework

$$LR = LR_{H_1, H_2}(E) = \frac{P(E | H_1)}{P(E | H_2)}$$

is the likelihood ratio for evidence E with respect to the two hypotheses H_1 and H_2 . The LR measures how much better H_1 explains the evidence E than H_2 .

Likelihood Ratio. Example



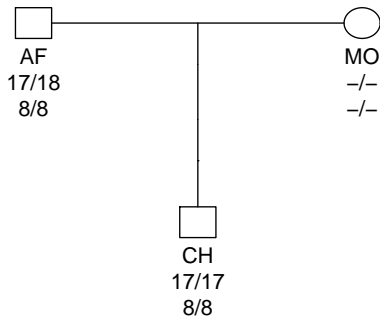
$$LR = \frac{P(E | H_1)}{P(E | H_2)} = \dots = \frac{P(g_{CH} | g_{AF})}{P(g_{CH})}$$

$$LR_1 = \frac{\frac{1}{2}p_{17}}{p_{17}^2} = \frac{1}{2 \times 0.204} = 2.45$$

$$LR_2 = \frac{p_8}{p_8^2} = \frac{1}{0.554} = 1.81$$

$$LR = LR_1 \times LR_2 = 2.45 \times 1.81 = 4.4.$$

Likelihood Ratio. Interpretation and assumptions



- ▶ Interpretation $LR=4.4$: The data is 4.4 times more likely if AF is assumed to be the father compared to the unrelated alternative.
- ▶ Assumptions
 - Hardy–Weinberg Equilibrium (HWE).
 - Independent markers.
 - No artefacts: (no mutation, no silent alleles, no drop-out/in, no error).

Realistic number of markers

Marker	CH	AF	LR	LR(mut)
D3S1358	17/17	17/18	2.45	2.45
TPOX	8/8	8/8	1.81	1.80
D6S474	16/17	14/15	0.000	0.001
...
D19S433	12/15	12/14	3.34	3.34
Total			0	25070642

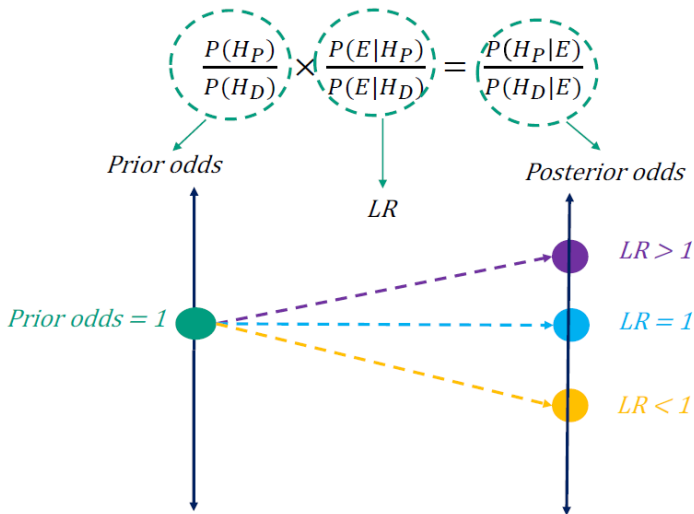
W = Posterior probability of paternity

- ▶ Assume *prior probabilities* $P(H_P) = P(H_D) = 0.5$ (*reasonable?*)
- ▶ *Prior odds* $\frac{P(H_P)}{P(H_D)} = 1$.

Then

$$\begin{aligned} W = P(H_P | E) &= \frac{LR}{LR + 1} = \frac{25070642}{25070642 + 1} \\ &= 0.99999996 = \text{"Probability of } H_P \text{ given evidence"} \end{aligned}$$

Bayes theorem on odds form



Blackstone ratio

- Blackstone's ratio:
 $(1 + c_2)/(1 + c_1) = 10$ (in practice much higher.)

		TRUTH	
		Guilt H_P	Innocence H_D
VERDICT	Guilt H_P	0	$1 + c_2$
	Innocence H_D	$1 + c_1$	0

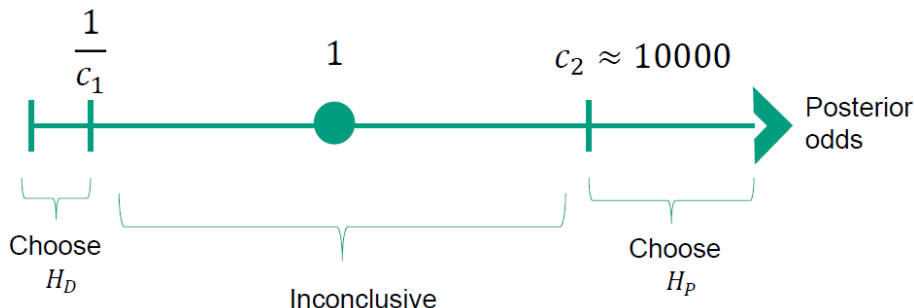
BETTER THAT TEN
GUILTY PERSONS ESCAPE
THAN THAT ONE
INNOGENT SUFFER

— SIR WILLIAM BLACKSTONE (1765)



Make no decision: cost = 1

Optimal decision rule




If c_1 and c_2 are specified, an optimal decision rule can be determined.

See Tillmar and Mostad (2014) for an application

Adding evidence I

- If prior odds = 0 or $LR = 0$

 posterior odds = 0

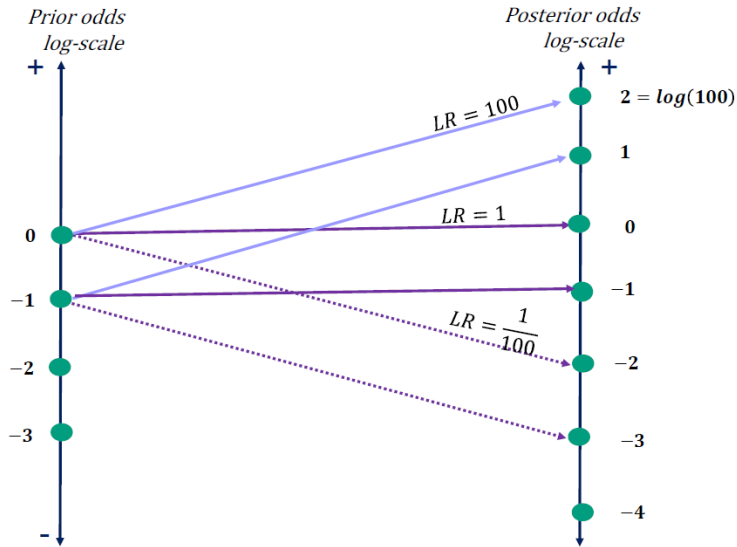
- Assume prior odds > 0 and $LR > 0$. Then

$$\log(\text{prior odds}) + \log(LR) = \log(\text{posterior odds})$$

- $\log(LR) = \log_{10}(LR)$ (unit called "ban" - Alan Turing)

*Good IJ (1985)

Adding evidence II



Theta correction. Dispute laid to rest

nature

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commentary

Nature **371**, 735 - 738 (27 October 2002); doi:10.1038/371735a0

DNA fingerprinting dispute laid to rest

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Forensic Science Research and Training Center, FBI Laboratory, FBI Academy, Quantico, Vi

Hardy Weinberg

Two alleles A, B .

$$p_A = 0.4, p_B = 0.6.$$

$$\text{Fraction } A/A: 0.4^2 = 0.160$$

$$\text{Fraction } A/B: 2 \cdot 0.4 \cdot 0.6 = 0.480$$

$$\text{Fraction } B/B: 0.6^2 = 0.360$$

$$\text{Sum} = 1.000$$

Problem: Above requires HW, not valid if 'unrelated people' are slightly related

Solution: theta-correction

Theta - correction

Homozygous $A, A: \theta p_A + p_A^2(1-\theta),$

Heterozygous $A, B: 2 p_A p_B(1-\theta).$

$\theta = 0.1$ (extreme case)

Fraction A/A: $0.1 * 0.4 + 0.4^2 * (1 - 0.1) = 0.184 > 0.160$

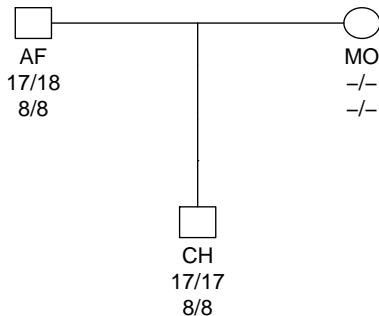
Fraction A/B: $2 * 0.4 * 0.6 * (1 - 0.1) = 0.432 < 0.480$

Fraction B/B: $0.1 * 0.6 + 0.6^2 * (1 - 0.1) = 0.384 > 0.360$

Sum 1.000 1.000

- Fraction homozygotes increases with θ

Previous example



$$LR_1 = \frac{\frac{1}{2}p_{17}}{p_{17}^2} = \frac{1}{2 \times 0.204} = 2.45$$

$$LR_2 = \frac{p_8}{p_8^2} = \frac{1}{0.554} = 1.81$$

$$LR = LR_1 \times LR_2 = 2.45 \times 1.81 = 4.4.$$

Fst=Theta=0.01. Input: Pedigrees > Parameters

Project name: Demo1 Number of pedi...

Pedig...	Pr...	Posterior	Likelihood ...	Ln like...
H1 AF ...	0.5	0.8020685	4.05225374	-6.87...
H2: un...	0.5	0.1979315	1	-8.27...

Set Parameters [X]

Theta (Fst) parameter: 0.01

Prior parameters

Generation parameter: 1

Maximum generations: 5

Inbreeding parameter: 1

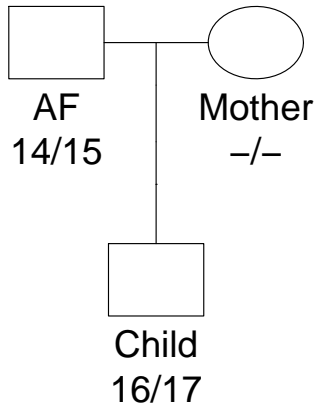
Promiscuity parameter: 1

Use Case-specific DNA data
☒ Yes ☐ No

Save Cancel

- ▶ $LR = 2.298 \cdot 1.764 = 4.1$ when $\theta = 0.01$
- ▶ $LR = 2.45 \cdot 1.81 = 4.4$ when $\theta = 0.00$.

Mutation: Exercise 2.2, 2.7



Mutation: Results, similar to Exercise 2.9

System	Child	AF	LR	LR(mut)
D3S1358	17/17	17/18	2.450	2.449
TPOX	8/8	8/8	1.805	1.804
D6S474	16/17	14/15	0.000	0.001
3 markers			0.000	0.0044

22 (1 mut)			0.000	25070642

Table 1: Genotype data for a Child and alleged father (AF) along with LR-s. The rightmost column is based on a stepwise unstationary mutation model (explained below) with mutation rate 0.001 and range 0.5 for all markers.

Equal model

Mutation to						
Al...	13	14	15	16	17	18
13	0.999	0.0002	0.0002	0.0002	0.0002	0.0002
14	0.0002	0.999	0.0002	0.0002	0.0002	0.0002
15	0.0002	0.0002	0.999	0.0002	0.0002	0.0002
16	0.0002	0.0002	0.0002	0.999	0.0002	0.0002
17	0.0002	0.0002	0.0002	0.0002	0.999	0.0002
18	0.0002	0.0002	0.0002	0.0002	0.0002	0.999

- ▶ $P(\text{no mutation}) = 0.999$
- ▶ **Problem:** $P(14 \rightarrow 17) = P(15 \rightarrow 16) = 0.0002$.

Mutation: Biology

- Mutation rate varies with
 - Sex of parent and locus.
- Alleles tend to mutate to close alleles:



- Several models
-
- Mutation rates:
<http://www.cstl.nist.gov/strbase/mutation.htm>

Mutation: Input

Mutation options

Male mutation model

Model: 3. Stepwise (Unstationary) ▼

Rate: 0.001

Range: 0.5

Rate 2:

Female mutation model

Model: 3. Stepwise (Unstationary) ▼

Rate: Same as Male
1. Equal probability (Simple)
2. Proportional to freq.
3. Stepwise (Unstationary)
4. Stepwise (Stationary)
5. Extended stepwise

Range:

Rate 2:

☐ Change model only

Apply to selected

Apply to all

Close

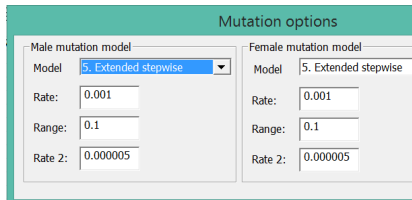
Mutation Matrix. Range

Mutation to						
Al...	13	14	15	16	17	18
13	0.999	0.000...	0.000258...	0.00012903	6.4516e-005	3.2258e-
14	0.0003...	0.999	0.000347...	0.00017391	8.6957e-005	4.3478e-
15	0.0001...	0.000...	0.999	0.00030769	0.00015385	7.6923e-
16	7.6923...	0.000...	0.000307...	0.999	0.00030769	0.000153
17	4.3478...	8.695...	0.000173...	0.00034783	0.999	0.000347
18	3.2258...	6.451...	0.000129...	0.00025806	0.00051613	0.999

$$\text{Range} = \frac{15 \rightarrow 17}{15 \rightarrow 16} = \frac{0.00015385}{0.00030769} = 0.5$$

Extended stepwise model:

Generally recommended, consistent for microvariants



Mutation options

Male mutation model		Female mutation model	
Model	5. Extended stepwise	Model	5. Extended stepwise
Rate:	0.001	Rate:	0.001
Range:	0.1	Range:	0.1
Rate 2:	0.000005	Rate 2:	0.000005

- ▶ **Rate Integer mutations:**
 $9 \rightarrow 10$, $9.3 \rightarrow 10.3$
- ▶ **Range:** As before.
1 step $1/0.1 = 10$ times more likely than two steps, etc.
- ▶ **Rate2 Fractional Mutations:**
 $9.3 \rightarrow 10$, $9 \rightarrow 9.3$

Extended stepwise model: Example

Mutation to					
A...	9	9.3	10	10.3	11
9	0.998995	2.5e-006	0.0009090909091	2.5e-006	9.090909091e-005
9.3	1.666666667e-006	0.998995	1.666666667e-006	0.001	1.666666667e-006
10	0.0005	2.5e-006	0.998995	2.5e-006	0.0005
10.3	1.666666667e-006	0.001	1.666666667e-006	0.998995	1.666666667e-006
11	9.090909091e-005	2.5e-006	0.0009090909091	2.5e-006	0.998995

- ▶ Recall: Rate = 0.001, Range = 0.1, Rate2 = 0.000005.
- ▶ Note: $P(\text{"no mut"}) = 1 - (0.001 + 0.000005) = 0.998995$.

$$P(9 \rightarrow 10) = 0.0009 >$$

$$P(9 \rightarrow 9.3) = 2.5e - 006 = 0.0000025$$

$$\frac{P(9 \rightarrow 11)}{P(9 \rightarrow 10)} = \frac{0.00009}{0.0009} = 0.1$$

Silent alleles. Input: General DNA data > ... > Options

The screenshot shows three overlapping windows from a forensic genetics software interface.

Options Window: Contains input fields for 'Silent Allele Frequency' (0.05), 'Database size' (2500), and 'Dropout' (0). It has 'Save' and 'Cancel' buttons.

Edit Marker Window: Has a 'System name' field with 'S1'. It contains a table with alleles and their frequencies.

Name	Frequency
Silent Allele	0.05
A	0.1
B	0.1
Extra allele	0.75

Buttons on the right: Save, Close, Options, Mutation models, Edit, Remove.

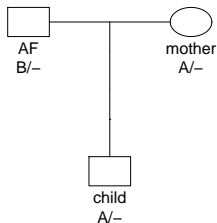
Add allele section:

Name	Frequency

Buttons: Add

Third Window (partially visible): Contains a vertical stack of buttons: Add, Edit, Remove, Mutations, Export, Import, and Close.

Exercise 2.11



- ▶ Enter genotypes as homozygous.
- ▶ $p_B = 0.1$, $p_S = P(\text{"Silent allele"}) = 0.05$. Now e.g.
- ▶ $P(B/-) = p_B^2 + 2 \cdot p_B p_S = 0.02$.
- ▶ Statistics for silent alleles:

<http://www.cstl.nist.gov/strbase/NullAlleles.htm>



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Academic Press, 2015.



IJ Good.

Weight of evidence: A brief survey.

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Choosing supplementary markers in forensic casework.

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